

Octopus: The Multisystem Framework

Micael Oliveira, Martin Lüders and the Octopus developers

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Motivation

At its core, Octopus [1] solves a set of differential equations describing the dynamics of a system of electrons and nuclei:

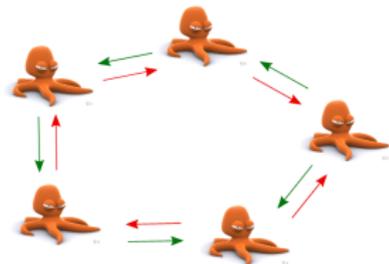
$$i \frac{\partial}{\partial t} \varphi_i(\mathbf{r}, t) = \left\{ v_{\text{ext}}(\mathbf{r}; \mathbf{R}) + v_{\text{Hxc}}[n](\mathbf{r}, t) \right\} \varphi_i(\mathbf{r}, t)$$
$$m_I \frac{\partial^2}{\partial t^2} \mathbf{R}_I(t) = \sum_{J \neq I} \mathbf{F}_{IJ}(\mathbf{R}_I, \mathbf{R}_J) + \mathbf{F}_{Ie}(\mathbf{R}_I; n)$$

- Electronic orbitals $\varphi_i(\mathbf{r}, t)$ are discretized on a grid
- Nuclei are treated classically as point charges
- The equations are coupled by the nuclear coordinates \mathbf{R} and by the electronic density $n(\mathbf{r}, t) = \sum_i |\varphi_i(\mathbf{r}, t)|^2$

Motivation

Developers wanted to couple new types of systems with electrons and ions:

- Classical electromagnetic fields (Maxwell equations)
- Quantized EM fields (quantum electrodynamics)
- Solvent models
- ...



This can be challenging:

- Very different numerical methods are used to solve each subset of equations
- Time-scales can be very different (e.g., electrons move faster than nuclei)

Motivation

The new framework should be able to:

- Handle arbitrary number of systems and system types
- Implement different types of interactions between systems
- Implement several different algorithms for each system type
- Decide what systems/interactions/algorithms to run from the input file
- Allow users to mix different types of algorithms (e.g., time-propagation and minimization)
- Give the user complete control over any possible approximations
- Allow for parallelization over systems

Very ambitious and not trivial to implement!

How to design this

- 1 Clearly state the problem we are trying to solve
- 2 Write down all requirements
- 3 Choose a suitable programming paradigm (object-oriented, functional, etc)
- 4 Develop and test the code using a simple, well understood example application that covers most of the intended use-cases

What problem are we trying to solve

- ~~Framework to simulate interacting physical systems~~
- ~~Framework to solve systems of coupled differential equations~~
- Framework to handle one or more iterative algorithms that need to exchange information at specific iterations

The framework needs to:

- Implement a mechanism for information exchange
- Implement conditions for information exchange
- Keep track of the internal state of systems, couplings, and algorithms

What problem are we trying to solve

Some terminology:

- **System**: physical system characterized by some internal quantities (e.g, positions, densities, temperatures, etc) that are updated by some iterative algorithm
- **Coupling**: an internal quantity of a system that is required to execute the
- **Interaction**: a term required to execute the algorithm of a system that, in general, requires internal quantities from the system and some couplings to be evaluated (e.g., gravitational force)
- **Interaction partner**: some entity that contains couplings needed by other systems. All systems can be interaction partners, but not all interaction partners are systems (e.g., data models)

Design requirements

Main requirement: framework plus all existing systems, interactions and algorithms should be easy to maintain and extend.

- Framework should be completely independent of existing systems, interactions and algorithms
- Adding new systems should not require modifying existing systems, interactions or algorithms
- Adding new interactions should only require to modify systems that want to use those interactions
- Adding new algorithms should only require to modify systems that want to use those algorithms
- Modifications to the framework should only be required when adding new **features**, not when adding new systems/interactions/algorithms

Programming paradigm and design choices

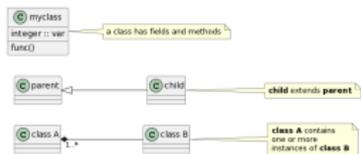
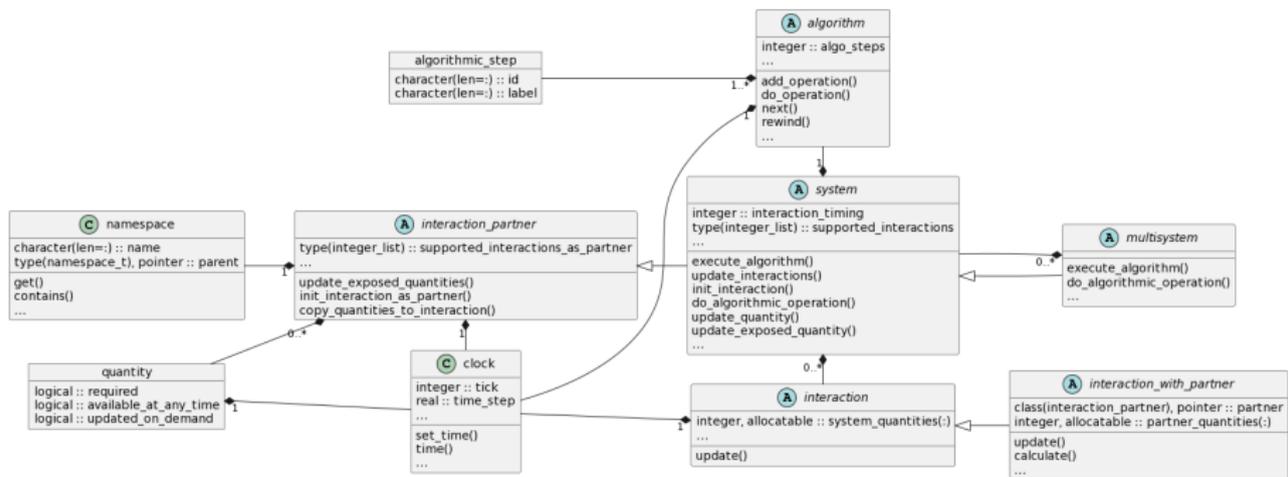
The way **NOT** to do it:

```
if (system_A%is_electrons) then
  ...
  select case (system_A%propagator)
  case (AETRS)
    ...
    if (system_A%has_interaction_X_with_system_B) then
      ...
    end if
  end select
  ...
else if (system_A%is_ions) then
  if ((system_A%has_interaction_Y_with_system_B) then
    ...
  end if
  ...
end if
```

Programming paradigm and design choices

- Object Oriented Programming
- Framework defines several abstract classes for systems, interactions and algorithms
 - Actual systems, interactions and algorithms provide implementations for the required deferred methods
 - Clean separation between the framework and the math/physics
- Systems do not know about each other directly, instead they know interactions
- An interaction connects a system with an interaction partner
- Interactions are uni-directional
- Algorithms are implemented as a set of state machine atomic operations (algorithmic operations)
- Systems do not inherit from the algorithms, instead, they implement algorithmic operations (Fortran does not allow multiple inheritance!)

UML Class diagram of the framework



The general algorithm

```
repeat  
  for all systems do  
    algo_op  $\leftarrow$  next algorithmic operation  
    break  $\leftarrow$  false  
    while not break do  
      if algo_op  $\neq$  update interactions then  
        execute algorithmic operation  
        algo_op  $\leftarrow$  next algorithmic operation  
      else  
        try updating interactions  
        if interactions updated then  
          algo_op  $\leftarrow$  next algorithmic operation  
        end if  
        break  $\leftarrow$  true  
      end if  
    end while  
  end for  
until all algorithms finished
```

Conditions for interaction update

When a system request an interaction to be updated, the following conditions must be met for a successful update:

- The necessary system quantities must be at the exact requested time
- The partner's algorithm clock must be at the requested time or is going to reach the requested time in the next time-step
- The necessary partner quantities must be either:
 - at the exact requested time (if user requested the interaction timing to be exact)
 - at the closest possible time in the past (if the user allowed for retarded interactions)
 - at the closest possible time in the future (if the user allowed for time interpolation)

Updating clocks

- The algorithm's clock is tentatively advanced when interactions are being updated and rewound if failed
- The algorithm's clock is advanced when interactions are successfully updated
- The system's clock is advanced when a time-step/iteration is finished
- A quantity's clock is updated whenever the quantity is updated

Design in practice (continued)

- Three general types of algorithmic operations:
 - System and algorithmic generic: implemented in the framework
 - Algorithm specific and system generic: implemented in the algorithm classes
 - System specific: implemented in the system classes
- The framework keeps track of time (iterations) with clocks (counters)
 - Systems, algorithms and quantities all have clocks attached
 - The algorithm's clock is advanced when interactions are being updated
 - The system's clock is advanced when a time-step/iteration is finished
 - A quantity's clock is updated whenever the quantity is updated